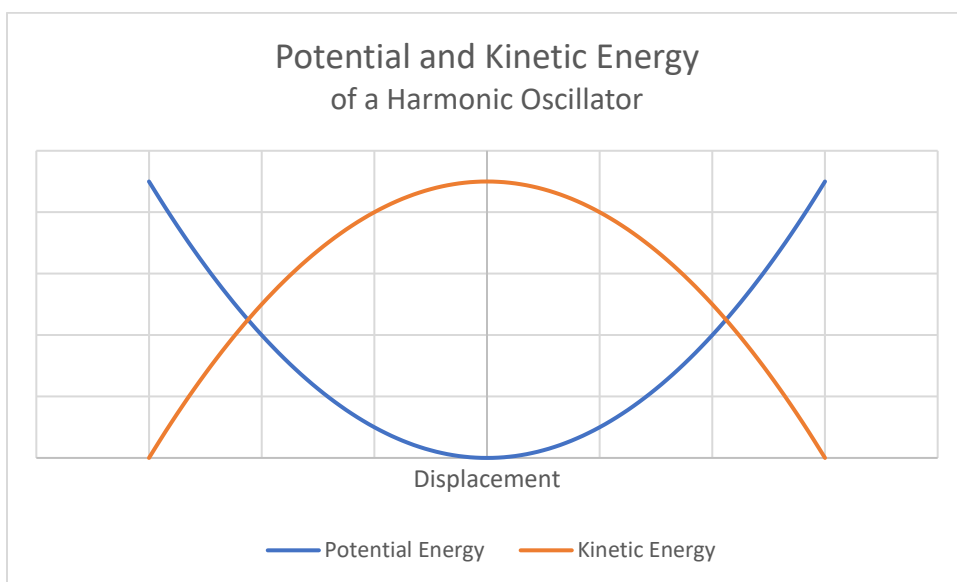


- Convert the temperatures indicated to complete the following table

°F	°C	K
77	25	298.15
98.6	37	310.15
212	100	373.15
-40	-40	233.15
32	0	273.15

- Make a graph representing the potential energy of a harmonic oscillator as a function of displacement from equilibrium. On the same graph, include a function describing the kinetic energy as a function of displacement from equilibrium as well as the total energy of the system.



- Calculate the work required to move a 3.2 kg mass 10.0 m against a resistive force of 9.80 N.

Work is given by the negative product of force and displacement.

$$w = -F \Delta x$$

So,

$$w = -(9.80 \text{ N})(10.0 \text{ m}) \left( \frac{\text{J}}{\text{N m}} \right) = -98.0 \text{ J}$$

- Calculate the work needed for a 22.4 L sample of gas to expand to 44.8 L against a constant external pressure of 0.500 atm.

The work of expansion of a gas against a constant external pressure is

$$w = -p_{\text{ext}}\Delta V$$

So

$$w = -(0.500 \text{ atm})(44.8 \text{ L} - 22.4 \text{ L}) = -11.2 \text{ atm L}$$

But what is an *atm L*? This can be converted to J using the ratio of the gas law constant expressed in appropriate units:

$$-(11.2 \text{ atm L}) \left( \frac{8.314 \frac{\text{J}}{\text{mol K}}}{0.08206 \frac{\text{atm L}}{\text{mol K}}} \right) = -11347.4 \text{ J} = -11.3 \text{ kJ}$$

Alternatively, one can convert to MKS units by recognizing that

$$\begin{aligned} 1 \text{ atm} &= 101325 \text{ Pa} \\ 1000 \text{ L} &= 1 \text{ m}^3 \\ 1 \text{ Pa m}^3 &= 1 \text{ J} \end{aligned}$$

So

$$-11.2 \text{ atm L} \cdot \frac{101325 \text{ Pa}}{1 \text{ atm}} \cdot \frac{\text{m}^3}{1000 \text{ L}} \cdot \frac{\text{J}}{\text{Pa m}^3} \cdot \frac{\text{kJ}}{1000 \text{ J}} = -11.3 \text{ kJ}$$

5. If the internal and external pressure of an expanding gas are equal at all points along the entire expansion pathway, the expansion is called “reversible.” Calculate the work of a reversible expansion for 1.00 mol of an ideal gas expanding from 22.4 L at 273 K to a final volume of 44.8 L.

The work of a reversible expansion (expressed in differential form) is given by

$$dw = -p dV$$

So, to get *w*, one must integrate!

$$w = - \int_{V_1}^{V_2} p dV$$

But pressure is very much dependent on volume for an ideal gas.

$$p = \frac{nRT}{V}$$

So

$$w = -nRT \int_{V_1}^{V_2} \frac{dV}{V}$$

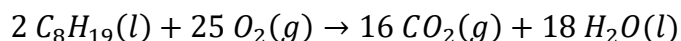
For an isothermal, reversible expansion. (If the gas was not ideal, a difference equation of state might be used to substitute for  $p$  in terms of  $V$ ,  $n$ ,  $R$ , and  $T$ .) After integration, the expression becomes

$$w = -nRT \ln \left( \frac{V_2}{V_1} \right)$$

Substituting the values from the problem,

$$\begin{aligned} w &= -(1.00 \text{ mol}) \left( 8.314 \frac{\text{J}}{\text{mol K}} \right) (273 \text{ K}) \ln \left( \frac{44.8 \text{ L}}{22.4 \text{ L}} \right) \\ &= -1573.3 \text{ J} \end{aligned}$$

6. The reaction of combustion of the gasoline (assuming it is composed of n-octane only) is given by the following chemical equation:



From the following table, calculate the total amount of energy available to drive a 1500 kg car by burning 40.0 L of gasoline, assuming 25% efficiency of converting the chemical energy in the fuel into mechanical (kinetic) energy of the car. The density of n-octane is 703 kg/m<sup>3</sup>.

Compound	$\Delta H_f$ (kJ/mol)	MW (g/mol)
C <sub>8</sub> H <sub>18</sub> (l)	-208.27	114.2285
O <sub>2</sub> (g)	0	31.9988
CO <sub>2</sub> (g)	-393.475	44.0095
H <sub>2</sub> O(l)	-285.828	18.01528

First, let's calculate the enthalpy of combustion for octane from the data provided.

$$\begin{aligned} \Delta H_c &= (16 \text{ mol}) \left( -393.457 \frac{\text{kJ}}{\text{mol}} \right) + (18 \text{ mol}) \left( -285.828 \frac{\text{kJ}}{\text{mol}} \right) - (2 \text{ mol}) \left( -208.27 \frac{\text{kJ}}{\text{mol}} \right) \\ &= -11023.676 \text{ kJ} \end{aligned}$$

This means that for every 2 mol of C<sub>8</sub>H<sub>18</sub>(l) combusted, 11023.676 kJ of energy will be released. Now, we just need to figure out how many mol of C<sub>8</sub>H<sub>18</sub>(l) there are in 40.0 L.

$$40.0 \text{ L} \cdot \frac{m^3}{1000 \text{ L}} \cdot \frac{703 \text{ kg}}{m^3} \cdot \frac{1000 \text{ g}}{\text{kg}} \cdot \frac{\text{mol } C_8H_{18}}{114.2285 \text{ g}} = 24\bar{6}.173 \text{ mol } C_8H_{18}$$

So, the total energy available, assuming 25% efficiency is given by

$$\left( 24\bar{6}.173 \text{ mol} \cdot \frac{11023.6\bar{7}6 \text{ kJ}}{2 \text{ mol}} \right) \left( \frac{25 \%}{100 \%} \right) = 339,216.424 \text{ kJ}$$